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equations are  $3^3 + 4^3 + 5^3 = 6^3$ ,  $1^3 + 6^3 + 8^3 = 9^3$ ,  $3^3 + 10^3 + 18^3 = 19^3$ ,

$$7^3 + 14^3 + 17^3 = 20^3, 4^3 + 17^3 + 22^3 = 25^3, 11^3 + 15^3 + 27^3 = 29^3.$$

Then the three positive integer numbers are  $x = \frac{11^3 + 15^3}{2}$ ,  $y = \frac{11^3 + 27^3}{2}$ ,

$z = \frac{15^3 + 27^3}{2}$ . Also  $x, y, z$  may be found from any equation, including the algebraic sum, for the sum of three cubes = a cube, by first multiplying each cube by  $2^3$ .

Also solved by *O. W. Anthony, H. W. Draughon, C. D. Schmitt, and G. B. M. Zerr.*

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## PROBLEMS.

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27. Proposed by J. W. NICHOLSON, LL. D., President and Professor of Mathematics, Louisiana State University and A. and M. College, Baton Rouge, Louisiana.

Required a formula for finding five integers the sum of whose cubes is a cube.

28. Proposed by DAVID E. SMITH, Ph. D., Professor of Mathematics, Michigan State Normal School, Ypsilanti, Michigan.

Decompose the product 97.673.257 into the sum of two fourth powers.

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## AVERAGE AND PROBABILITY.

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Conducted by B.F.FINKEL, Kidder, Missouri. All Contributions to this department should be sent to him.

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## SOLUTIONS OF PROBLEMS.

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13. Proposed by I. L. BEVERAGE, Monterey, Virginia.

Find the mean values of the roots of the quadratic  $x^2 - ax + b = 0$ , the roots being known to be real, but  $b$  being unknown and positive.

Solution by P. S. BERG, Apple Creek, Ohio, and JOHN DOLMAN, Jr., Counsellor-at-law, Philadelphia, Penn., and J. M. OULAW, A. M., Principal of High School, Monterey, Virginia.

Solving the given equation,  $x = \frac{1}{2}a \pm \sqrt{(\frac{1}{4}a^2 - b)}$ .

Therefore, if  $b$  be positive and  $x$  real,  $b$  cannot exceed  $\frac{1}{4}a^2$ . If  $\beta$  be the smaller of the two roots, its mean value, therefore, is

$$(1 \div \frac{1}{4}a^2) \int_0^{\frac{1}{2}a^2} \beta db = \frac{4}{a^2} \int_0^{\frac{1}{2}a^2} (\frac{1}{2}a + \sqrt{(\frac{1}{4}a^2 - b)}) db = \frac{4}{a^2} [\frac{1}{2}ab]_0^{\frac{1}{2}a^2} + \frac{4}{a^2} [\frac{1}{3} \sqrt{(a^2 - 4b)^3}]_0^{\frac{1}{2}a^2}$$

$$- \frac{a}{3} = \frac{a}{2} - \frac{a}{3} = \frac{1}{6} a.$$

The mean value of the larger root is, therefore,  $\frac{5}{6} a$ .

Also solved in a similar manner by *Professors Matz, Zerr, and Draughon*.

**14. Proposed by CHARLES E. MYERS, Canton, Ohio.**

$\frac{1}{3}$  of all the melons in a patch are not ripe, and  $\frac{1}{4}$  of all the melons in the same patch are rotten, the remainder being good. If a man enters the patch on a dark night and takes a melon at random, what is the probability that he will get a good one?

**Solution by H. W. DRAUGHON, Ohio, Mississippi, and G. B. M. ZERR, A. M., Principal of High School, Staunton, Virginia.**

Let  $12n$  = the whole number of melons in the patch. Then  $4n$  are not ripe and  $3n$  are rotten. The  $3n$  rotten melons may be included in the  $4n$  not ripe melons in which case there would be  $8n$  good melons, or the  $3n$  rotten may not be included in the  $4n$  not ripe melons in which case there would be  $12n - (3n + 4n) = 5n$  good melons.

$\therefore$  there cannot be less than  $5n$  nor more than  $8n$  good melons.

$$\therefore \text{ the chance of a good one} = \frac{1}{2} \left( \frac{5n + 8n}{12n} \right) = \frac{13}{24}.$$

$$\text{The chance of a not ripe one} = \frac{1}{2} \left( \frac{n + 4n}{12n} \right) = \frac{5}{24}.$$

$$\text{The chance of a rotten one} = \frac{1}{2} \left( \frac{0 + 3n}{12n} \right) = \frac{1}{8}.$$

$$\text{The chance of a not ripe and rotten one} = \frac{1}{2} \left( \frac{0 + 3n}{12n} \right) = \frac{1}{8}.$$

$$\therefore \frac{13}{24} + \frac{5}{24} + \frac{1}{8} + \frac{1}{8} = 1 \text{ as it should be.}$$

Solutions of this problem were received from *P. S. Berg, F. P. Matz, J. M. Colaw*.

**15. Proposed by F. P. MATZ, M. Sc., Ph. D., Professor of Mathematics and Astronomy in New Windsor College, New Windsor, Maryland.**

Todhunter proposes: "From a point in the circumference of a circular field a projectile is thrown at random with a given velocity, which is such that the diameter of the field is equal to the greatest range of the projectile: prove the chance of its falling within the field, is  $C = 2^{-1} - 2\pi^{-1}(\sqrt{2} - 1)$ , = .236+." Is this result perfectly correct as to fact?

**First Solution by the PROPOSER.**

Let  $P$  be the point from which the projectile is thrown,  $AP = 2a$ , and  $\angle APB = \theta$ . Now, if  $\phi$  = the angle of elevation at which the projectile is thrown, and  $C$  = the chance for any given value of  $\theta$ ; then, evidently, the required chance becomes